

Name: Key

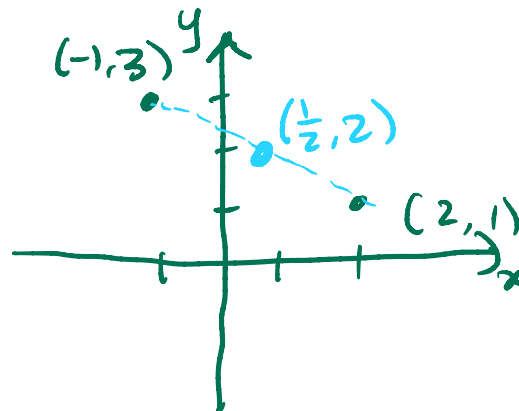
GTID: \_\_\_\_\_

Answer the questions in the spaces provided and BOX your answer. Organize and show your work for full credit.

- 1a. Find the midpoint between  $(-1, 3)$  and  $(2, 1)$ .

*Hint: use a sketch to check your answer.*

$$\begin{aligned} \text{midpoint is } & \left( \frac{x_1+x_2}{2}, \frac{y_1+y_2}{2} \right) \\ & = \left( \frac{-1+2}{2}, \frac{3+1}{2} \right) \\ & = \boxed{\left( \frac{1}{2}, 2 \right)} \end{aligned}$$



- 1b. Find the equation of the line passing through  $(-1, 3)$  and  $(2, 1)$ .

*Hint: these are the same points from #1a.*

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{1 - 3}{2 - (-1)} = \frac{-2}{3}$$

$$y = -\frac{2}{3}x + \frac{7}{3}$$

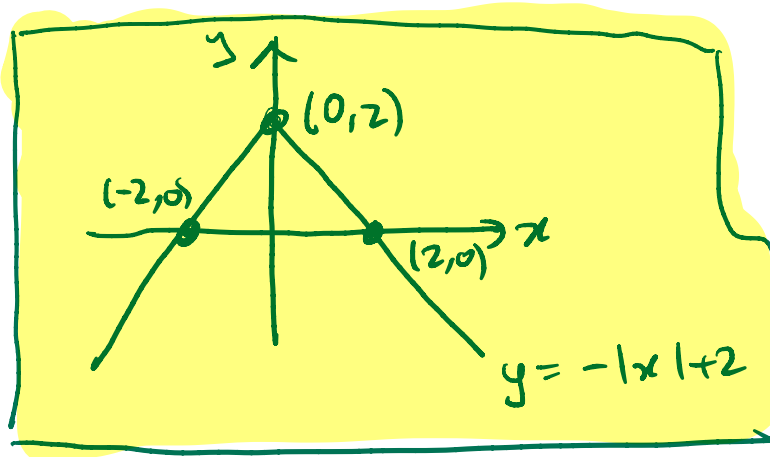
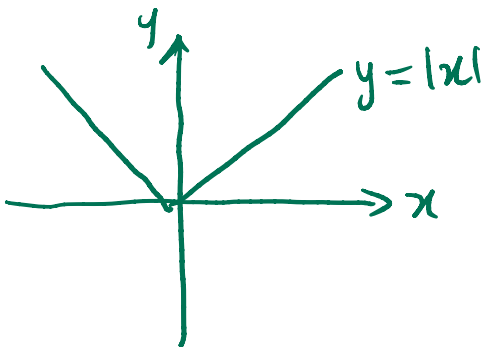
$$y = -\frac{2}{3}x + b \quad \text{plug in } (-1, 3)$$

$$3 = -\frac{2}{3}(-1) + b \Rightarrow 3 = \frac{2}{3} + b \quad b = 3 - \frac{2}{3}$$

$$\begin{aligned} &= \frac{9-2}{3} \\ &= \frac{7}{3} \end{aligned}$$

2. Graph:  $y = -|x| + 2$

*Hint: transform the graph of  $y = |x|$  using the techniques from class.*



3. Find the domain of  $f(x) = \frac{x^2-9}{\sqrt{4-x}}$ .

need  $4-x \geq 0 \Rightarrow x \leq 4$

and also  $\sqrt{4-x} \neq 0 \Rightarrow 4-x \neq 0 \Rightarrow x \neq 4$ .

So if  $x \leq 4$  and  $x \neq 4$ , then

$$D: x < 4$$

or  $D: (-\infty, 4)$

4. Suppose  $f(x) = x^2 - x + 1$  and  $g(x) = \sqrt{x-1}$ , and find  $f(g(5))$ .

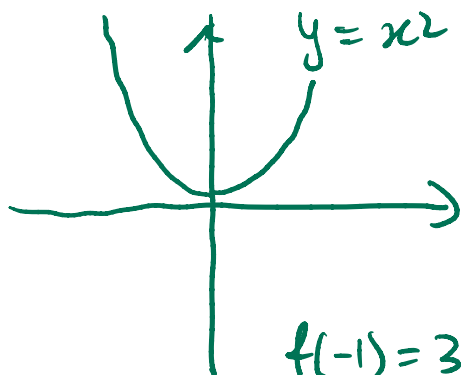
$$g(5) = \sqrt{5-1} = \sqrt{4} = 2$$

$$f(g(5)) = f(2) = 2^2 - 2 + 1 = 4 - 2 + 1 = 3$$

$$f(g(5)) = 3$$

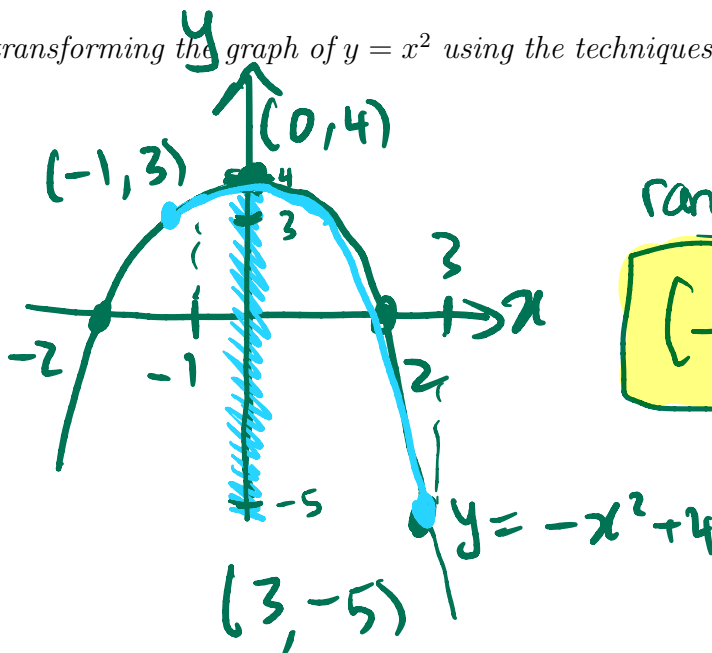
5. Given the function  $f(x) = -x^2 + 4$  with domain  $D: [-1, 3]$ , what is the range of the function on this interval?

Hint: sketch the function by transforming the graph of  $y = x^2$  using the techniques from class.



$$f(-1) = 3$$

$$f(3) = 5$$



range is

$$[-5, 4]$$