

Name: Key

GTID: _____

Answer the questions in the spaces provided and put your answer in the BOX. Organize work clearly and simplify answers for full credit.

1a. Convert 150° to radians.

$$150^\circ * \frac{\pi}{180^\circ} = \frac{150}{180} \pi = \frac{5}{6} \pi$$

$$= \boxed{\frac{5\pi}{6}}$$

$$\frac{5\pi}{6}$$

1b. Find the angle between 0° and 360° which is coterminal to 780° .

$$780^\circ - 360^\circ = 420^\circ$$

$$420^\circ - 360^\circ = 60^\circ$$

$$60^\circ$$

1c. Find the exact value of $\cos(\pi) - \sin(\frac{\pi}{2})$.

$$\cos(\pi) = -1$$

$$\sin(\frac{\pi}{2}) = 1$$

$$-1 - 1 = -2$$

$$\begin{array}{c} \uparrow \\ \pi \\ \leftarrow \\ \hline \rightarrow \\ \hline \uparrow \\ \frac{\pi}{2} \\ \leftarrow \\ \hline \rightarrow \\ \hline \end{array}$$

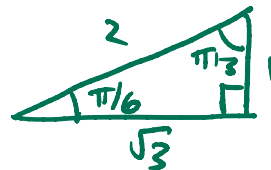
$$-2$$

1d. State the range of $f(x) = 3 \csc(2x)$.range of $y = \csc x$ is $\mathbb{R} = (-\infty, -1] \cup [1, \infty)$ same as range $y = \csc(2x)$ (horizontal compression)So range of $y = 3 \csc(2x)$ is $(-\infty, -3] \cup [3, \infty)$

$$(-\infty, -3] \cup [3, \infty)$$

2. Find the six trigonometric values of $\frac{\pi}{6}$.

Note: clearly label each answer.



$$\begin{aligned} \sin\left(\frac{\pi}{6}\right) &= \frac{1}{2} & \csc\left(\frac{\pi}{6}\right) &= 2 \\ \cos\left(\frac{\pi}{6}\right) &= \frac{\sqrt{3}}{2} & \sec\left(\frac{\pi}{6}\right) &= \frac{2}{\sqrt{3}} \\ \tan\left(\frac{\pi}{6}\right) &= \frac{1}{\sqrt{3}} & \cot\left(\frac{\pi}{6}\right) &= \sqrt{3} \end{aligned}$$

3. Find all values of u so that the given point is on the unit circle $(\frac{-1}{3}, u)$. Show work for credit.

$$\left(\frac{-1}{3}\right)^2 + u^2 = 1$$

$$\Rightarrow u^2 = 1 - \frac{1}{9}$$

$$\Rightarrow u^2 = \frac{8}{9}$$

$$\Rightarrow u = \pm \sqrt{\frac{8}{9}}$$

$$\Rightarrow u = \pm \frac{\sqrt{8}}{3}$$

$$\begin{aligned} \sqrt{8} &= \sqrt{2 \cdot 4} \\ &= 2\sqrt{2} \end{aligned}$$

So $u = \pm \frac{\sqrt{2}}{3}$

4. Graph $f(x) = \sin(2x)$ and include all x -values in the range $[-\frac{\pi}{2}, \pi]$ in your sketch.

Note: label any intercepts, label the axes and the curve, and identify and include a total of at least **six** points on your graph for full credit.

