

1. Integrate $\int (x+1) \ln(x^2) dx$.

2. Integrate $\int (2x+1) \ln(x^2+x) dx$.

3. Find the length of the curve $y = \frac{x^3}{12} + \frac{1}{x}$, $1 \leq x \leq 4$.

4. A jellybean cross-section through the middle is an oval with equation

$$9x^2 + 4y^2 = 36.$$

Find the volume of the jellybean.

5. Integrate $\int \frac{dx}{x\sqrt{1+(\ln x)^2}}$.

6. Integrate $\int x^3 \sqrt{1-x^2} dx$.

7. The force required to move a heavy box decreases rapidly once the box starts moving. The force needed is

$$F(x) = \frac{1}{e^x - e^{-x}}$$

where $x \geq 1$ is the distance from start (we ignore the first 1 unit of movement).
Find the work needed to move the box from $x = 1$ to $x = \ln 10$.

8. Integrate $\int \frac{x+1}{(x+2)^2} dx$.

9. Integrate $\int \frac{2x+5}{(x+2)(x+3)} dx$.

10. Integrate $\int \frac{x+4}{x^2+5x-6} dx$.