Math 1501

Instructor: Sal Barone

Name: _____

GT username: _____

- 1. No books or notes are allowed.
- 2. You may use ONLY NON-GRAPHING and NON-PROGRAMABLE scientific calculators. All other electronic devices are not allowed.
- 3. Show all work and fully justify your answer to receive full credit.
- 4. Please BOX your answers.
- 5. Good luck!

| Page | Max. Possible | Points |
|-------|---------------|--------|
| 1 | 30 | |
| 2 | 30 | |
| 3 | 20 | |
| 4 | 20 | |
| Total | 100 | |

1. During an experiment the velocity of a particle at time t is given by

$$(15 \text{ pts.})$$

$$v(t) = \frac{3t}{(1+t^2)^2}$$

for t > 0. How far has the particle travelled in the first 2 seconds of the experiment?

2. Solve the separable differential equation.

(15 pts.)

$$\frac{dy}{dx} = x^2 \sqrt{y}, \quad y > 0.$$

3. Find the value of the definite integral. *Hint: try integration by parts.*

$$\int_{1}^{e} x^{3} \ln(x) \, dx$$

(15 pts.)

4. Find the area bounded by the two curves $y = x^3 - 2x^2 + 1$ and y = 3x + 1. (15 pts.)

5. Integrate using any method.

$$(10 \text{ pts. each})$$

(a)
$$\int \tan(3x) dx$$

(b)
$$\int (4x - 3 + \sec^2(x)) dx$$

6. Find the value.

7.
$$\int_0^{\pi/4} \sec(x) \, dx$$

(10 pts. each)

8.
$$\int_0^1 \frac{1}{\sqrt{1-x^2}} \, dx$$