| Math 1552 Summer 2023 Exam 3 Practice | | | Name (Print): Canvas email: | | | | | | | |
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| Time limit: 75 Minutes | | | Teaching Assistant/Section: | | | | | | | |
| CT ID. | | | | | | | | | | _ |

By signing here, you agree to abide by the **Georgia Tech Honor Code**: I commit to uphold the ideals of honor and integrity by refusing to betray the trust bestowed upon me as a member of the Georgia Tech Community.

| Sign | Your | Name: | |
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Student Instructions

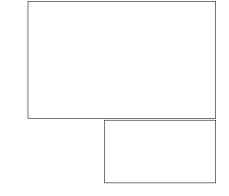
- Show your work and justify your answers for all questions unless stated otherwise.
- Organize your work in a reasonably neat and coherent way.
- Simplify your answers unless explicitly stated otherwise.
- Fill in circles completely. Do not use check marks, X's, or any other marks.
- Place a box around your final answer for full credit.
- Calculators, notes, cell phones, books are not allowed.
- Use dark and clear writing: your exam will be scanned into a digital system.
- Exam pages are double sided. Be sure to complete both sides.
- Leave a 1 inch border around the edges of exams.
- The last page is for scratch work. Please use it if you need extra space.
- This exam has 6 pages of questions.

1. (3 points) Which of the following statements are true? You do not have to show your work.

true false

- $\bigcirc \qquad \bigcirc \qquad \text{The alternating series } \sum_{n=1}^{\infty} (-1)^n \frac{n+3}{n+4} \text{ diverges.}$
- $\bigcirc \qquad \qquad \bigcirc \qquad \text{The radius of convergence of the power series } \sum_{n=0}^{\infty} \frac{3^n}{n!} (x-2)^n \text{ is } R = \infty.$
- $\bigcirc \qquad \qquad \bigcirc \qquad \text{The value of } e^{-1} \text{ is within an error of } \tfrac{1}{24} \text{ to } 1 \tfrac{1}{1!} + \tfrac{1}{2!} \tfrac{1}{3!}.$
 - 2. (5 points) State the Taylor series at x = 0 for the function and give the interval of convergence. You do not have to show work for this problem. *Hint: this is a common Taylor series.*

$$f(x) = \ln(1+x)$$



3. (8 points) Find the Taylor series at x=0 for the given function. If you use a common Taylor series state the series you are using.

$$f(x) = x^2 e^{-x}$$

4. (8 points) Determine if the given series converges or diverges. Show your work and clearly justify your answer for credit. Hint: try a comparison test. Use $\ln n \le \sqrt{n}$ if $n \ge 4$.

$$\sum_{n=4}^{\infty} \frac{3}{\sqrt{n} \ln n}$$

5. (8 points) Determine if the given series converges or diverges. Show your work and clearly justify your answer for credit.

$$\sum_{n=1}^{\infty} \frac{e^n}{n^e}$$

- 6. (8 points) Consider the function $f(x) = \sqrt{x}$.
 - (a) Find the Taylor polynomial $P_3(x)$ of degree N=3 expanded at x=1 (in powers of x-1).

(b) Use the formula below to find the maximum error of using $P_3(2)$, the Taylor polynomial evaluated at x=2, to approximate $f(2)=\sqrt{2}$.

$$|R_N(x)| \le \max |f^{(N+1)}(c)| \frac{|x-a|^{N+1}}{(N+1)!}$$

- 7. (10 points) Consider the power series $f(x) = \sum_{n=0}^{\infty} \frac{2^n}{n!} x^n$.
 - (a) Find the interval of convergence of the power series f(x). Hint: don't forget to test the endpoints separately.



(b) Find a power series for f'(x).



This page may be used for scratch work. Please indicate clearly on the problem if you would like your work on this page to be graded. Loose scrap paper is not permitted.

This page must **not** be detached from your exam booklet at any time.