## 1552 Homework Checks 3: Questions

June 21, 2023

## 1 Question 1: Improper Integral

Evaluate the improper integrals if they converge, or show that the integral diverges.
(Hint1: Evaluation of improper integrals should have limits - any solution without limits will not receive credit.
Hint2: Use L'Hopital's rule whenever applicable)

1. $\int_{0}^{\infty} x^{2} e^{-x} d x$
2. $\int_{0}^{4} \frac{x}{\left(x^{2}-1\right)^{2 / 3}} d x$

## 2 Question 2: Sequences

For the sequence below,
(a) find the l.u.b. and g.l.b.
(b) determine if the sequence is monotonic
(c) find the limit of the sequence
(d) determine whether the sequence converges or diverges.

1. $\left\{\frac{n+1}{2 n}\right\}$
2. $\left\{(-1)^{n} \frac{1}{5^{n}}\right\}$
