

## Quiz 4 (12 pm)

1. Let  $T : \mathbb{R}^2 \rightarrow \mathbb{R}^2$  be the linear transformation which associates to each  $\mathbf{x} \in \mathbb{R}^2$  the vector obtained from  $\mathbf{x}$  by first reflecting  $\mathbf{x}$  about the horizontal  $x$ -axis and then rotating  $\mathbf{x}$  by  $90^\circ$  clockwise. Find the standard matrix  $A$  of  $T$  as well as the image  $T\left(\begin{bmatrix} 1 \\ 1 \end{bmatrix}\right)$ . *Hint: the first column of  $A$  is  $T\left(\begin{bmatrix} 1 \\ 0 \end{bmatrix}\right)$  and the second column of  $A$  is  $T\left(\begin{bmatrix} 0 \\ 1 \end{bmatrix}\right)$ .* (4 pts. ea.)

2. Determine whether the given vectors are linearly independent or linearly dependent. If the vectors are linearly dependent find a non-trivial linear combination of the vectors which give the zero vector. (8 pts.)

$$\begin{bmatrix} 3 \\ -1 \\ 0 \end{bmatrix}, \begin{bmatrix} 1 \\ 1 \\ 2 \end{bmatrix}, \begin{bmatrix} 7 \\ -1 \\ 2 \end{bmatrix}$$

3. True or False section. (1 pt. each)

T/F If  $A$  is a  $4 \times 3$  matrix with 3 pivots, then the columns of  $A$  are linearly independent.

T/F If  $Ax = 0$  has the trivial solution, then the columns of  $A$  are linearly independent.

T/F If the columns of  $A$  are linearly independent, then  $Ax = b$  has a unique solution.

T/F The linear transformation with standard matrix  $\begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$  rotates vectors in  $\mathbb{R}^2$  by  $90^\circ$  counter-clockwise.