

Midterm 3 Lecture Review Activity, Math 1554

1. Indicate **true** if the statement is true, otherwise, indicate **false**.

	true	false
a) If S is a two-dimensional subspace of \mathbb{R}^{50} , then the dimension of S^\perp is 48.	<input type="radio"/>	<input type="radio"/>
b) An eigenspace is a subspace spanned by a single eigenvector.	<input type="radio"/>	<input type="radio"/>
c) The $n \times n$ zero matrix can be diagonalized.	<input type="radio"/>	<input type="radio"/>
d) A least-squares line that best fits the data points $(0, y_1), (1, y_2), (2, y_3)$ is unique for any values y_1, y_2, y_3 .	<input type="radio"/>	<input type="radio"/>

2. If possible, give an example of the following.

2.1) A matrix, A , that is in echelon form, and $\dim((\text{Row } A)^\perp) = 2$, $\dim((\text{Col } A)^\perp) = 1$

2.2) A singular 2×2 matrix whose eigenspace corresponding to eigenvalue $\lambda = 2$ is the line $x_1 = 2x_2$. The other eigenspace of the matrix is the x_2 axis.

2.3) A subspace S , of \mathbb{R}^4 , that satisfies $\dim(S) = \dim(S^\perp) = 3$.

2.4) A 2×3 matrix, A , that is in RREF. $(\text{Row } A)^\perp$ is spanned by $\begin{pmatrix} 2 \\ 3 \\ 1 \end{pmatrix}$.

3. Circle **possible** if the set of conditions are create a situation that is possible, otherwise, circle **impossible**. For the situations that are possible give an example.

3.1) A is $n \times n$, $A\vec{x} = A\vec{y}$ for a particular $\vec{x} \neq \vec{y}$, \vec{x} and \vec{y} are in \mathbb{R}^n , and $\dim((\text{Row } A)^\perp) \neq 0$.

possible **impossible**

3.2) A is $n \times n$, $\lambda \in \mathbb{R}$ is an eigenvalue of A , and $\dim((\text{Col}(A - \lambda I))^\perp) = 0$.

possible **impossible**

3.3) $\text{proj}_{\vec{v}}\vec{u} = \text{proj}_{\vec{u}}\vec{v}$, $\vec{v} \neq \vec{u}$, and $\vec{u} \neq \vec{0}$, $\vec{v} \neq \vec{0}$.

possible **impossible**

4. Consider the matrix A .

$$A = \begin{pmatrix} 1 & -3 & 0 & 2 \\ 0 & 0 & 1 & -3 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

Construct a basis for the following subspaces and state the dimension of each space.

4.1) $(\text{Row } A)^\perp$

4.2) $\text{Col } A$

4.3) $(\text{Col } A)^\perp$