

Taker Name:

Key

GTID: 90

Section:

Grader #1:

GTID: 90

PA#3B- §14.3: Partial derivatives

Find the total derivative Df of the function $f(r, s, t) = \begin{bmatrix} st^2 + re^{3s} \\ t \tan(rs) \end{bmatrix}$.

$$x(r, s, t) = st^2 + re^{3s}$$

$$y(r, s, t) = t \tan(rs)$$

$$Df = \begin{bmatrix} x_r & x_s & x_t \\ y_r & y_s & y_t \end{bmatrix}$$

$$x_r = 0 + e^{3s} = e^{3s}$$

$$x_s = t^2 + rs e^{3s}$$

$$x_t = 2st$$

$$y_r = st \sec^2(rs)$$

$$y_s = rt \sec^2(rs)$$

$$y_t = \tan(rs)$$

So

$$Df = \begin{bmatrix} e^{3s} & t^2 + rs e^{3s} & 2st \\ st \sec^2(rs) & rt \sec^2(rs) & \tan(rs) \end{bmatrix}$$

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G2:

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G3:

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