## Quiz 10

For the problems below consider the following graph $\mathcal{G}$ whose model is given below:


1. Determine if the graph is planar or not. If it is planar, give a planar model. If it is not planar, find a subgraph $\mathcal{H}$ and indicate whether it is homeomorphic to $K_{5}$ or $K_{3,3}$.
2. Let $\mathcal{H}$ be the subgraph of $\mathcal{G}$ obtained by deleting the vertex $g$ and the edge $(g, a)$. Determine whether $\mathcal{H}$ is Eulerian and/or Hamiltonian. Find a Eulerian circuit and/or a Hamiltonian cycle, if possible, or state that it is not possible.
3. Find the chromatic number $\chi(\mathcal{G})$ and give a $\chi(\mathcal{G})$-coloring of $\mathcal{G}$.
